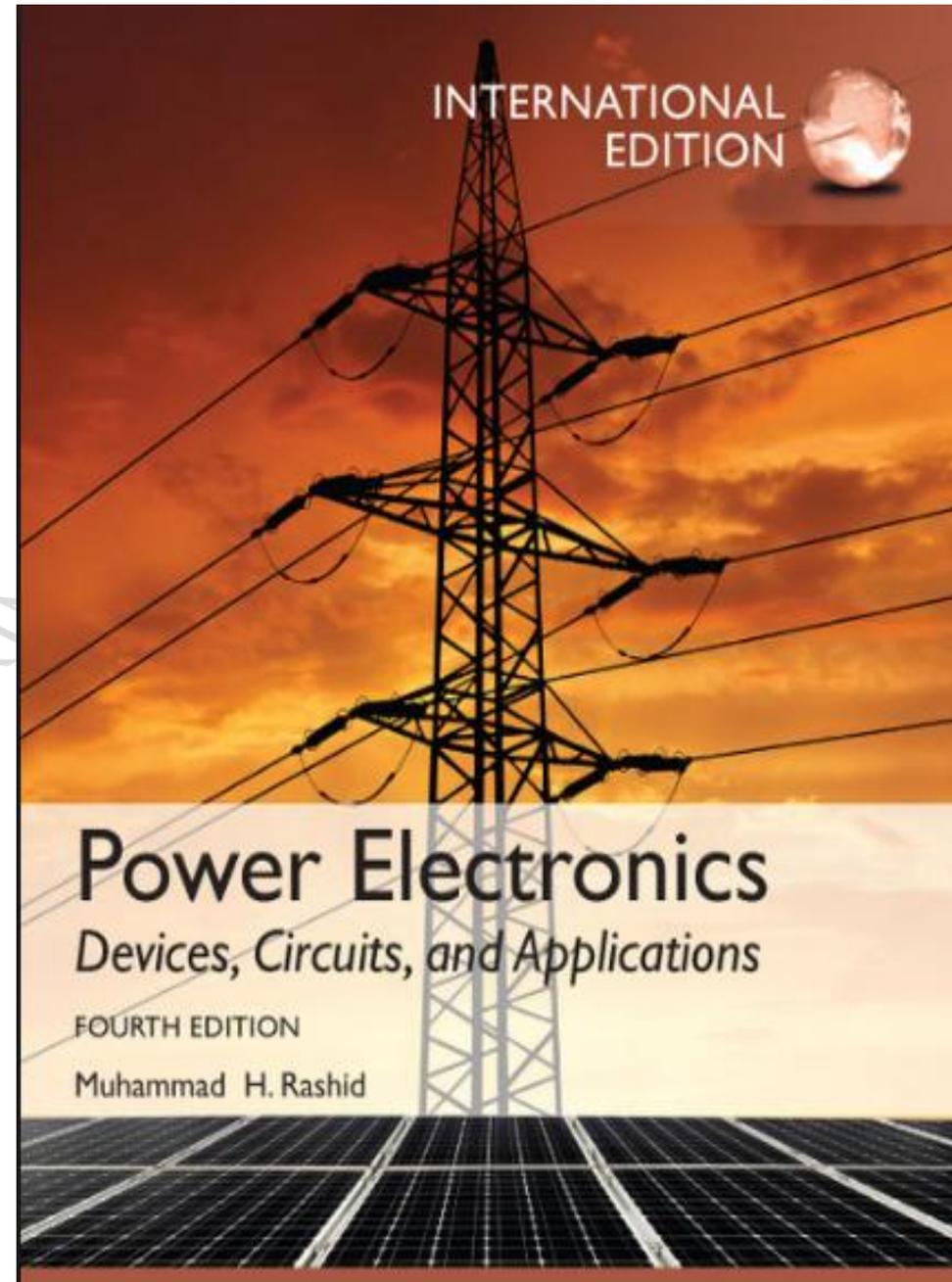


**University of Technology**  
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**Power Electronics/2018-2019)**  
**For the third years (Laser Engineering)**

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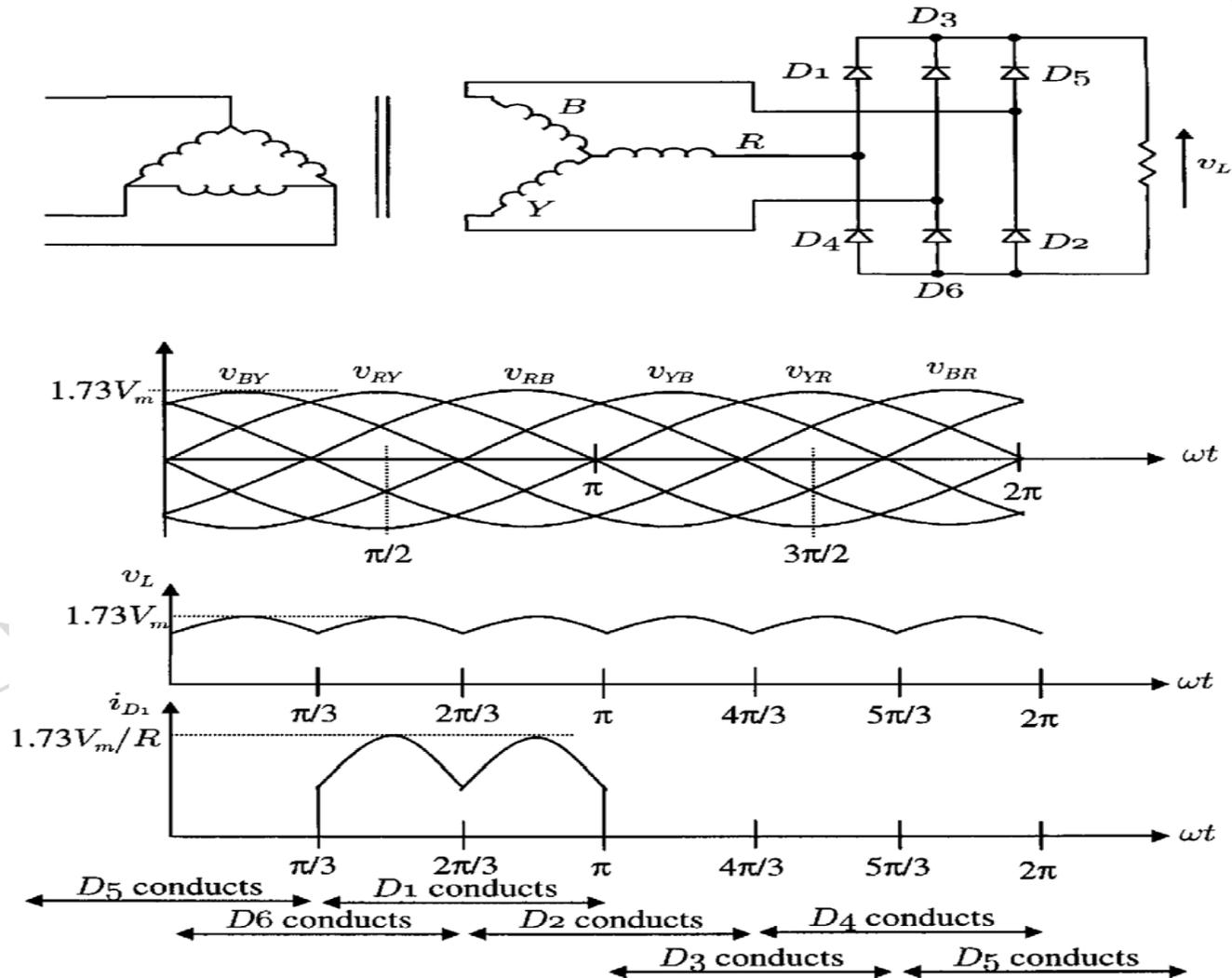


***Ref: Power Electronics 4<sup>th</sup> edition/ Muhammed H. Rashid***

# Lecture No.9

## Three-Phase Bridge Rectifiers

Three-phase bridge rectifiers are commonly used for high power applications because they have the highest possible transformer utilization factor for a three-phase system.



The diodes are numbered in the order of conduction sequences and the conduction angle of each diode is  $2\pi/3$ . The conduction sequence for diodes is **12, 23, 34, 45, 56, and 61**. The line voltage is **1.73** times the phase voltage of a three-phase star-connected source.

The average values of the output can be found as:

$$V_{dc} = \frac{6}{2\pi} \int_{\pi/3}^{2\pi/3} \sqrt{3} V_m \sin \theta d\theta$$

Or,

$$V_{dc} = V_m \frac{3\sqrt{3}}{\pi} = 1.654 V_m$$

Similarly, the rms value of the output voltage can be found as:

$$V_L = \sqrt{\frac{9}{\pi} \int_{\pi/3}^{2\pi/3} (V_m \sin \theta)^2 d\theta}$$

Or,

$$V_L = V_m \sqrt{\frac{3}{2} + \frac{9\sqrt{3}}{4\pi}} = 1.655 V_m$$

The rms current in each transformer secondary winding can also be found as:

$$I_s = I_m \sqrt{\frac{2}{\pi} \left( \frac{\pi}{6} + \frac{\sqrt{3}}{4} \right)} = 0.78 I_m$$

The rms current through a diode is:

$$I_D = I_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{6} + \frac{\sqrt{3}}{4} \right)} = 0.552 I_m$$

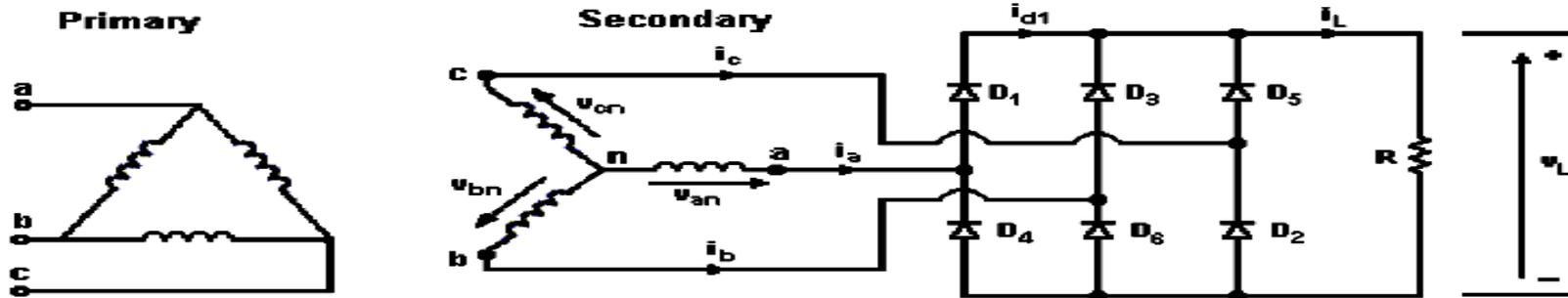
Where,  $I_m = 1.73 V_m/R$ .

- The dc output voltage is slightly lower than the peak line voltage or 2.34 times the rms phase voltage.
- The Peak Repetitive Reverse Voltage ( $V_{RRM}$ ) rating of the employed diodes is 1.05 times the dc output voltage.
- The Peak Repetitive Forward Current ( $I_{FRM}$ ) rating of the employed diodes is 0.579 times the dc output current.

**Example 3.4**

A three-phase rectifier has a purely resistive load of R. Determine

- a. The efficiency
- b. The form factor
- c. The rripple factor



**Solution**

a. Efficiency,

$$\eta = \frac{P_{dc}}{P_L}$$

Now:

$$P_{dc} = V_{dc} \times I_{dc} \quad P_L =$$

Since:

$$V_L \times I_L$$

$$V_{dc} = V_m \frac{3\sqrt{3}}{\pi} = 1.654 V_m$$

$$I_{dc} = \frac{V_{dc}}{R} = \frac{1.654 V_m}{R}$$

$$V_L = V_m \sqrt{\frac{3}{2} + \frac{9\sqrt{3}}{4\pi}} = 1.655 V_m$$

$$I_L = \frac{V_L}{R} = \frac{1.655 V_m}{R}$$

$$\eta = \frac{(1.65 V_m)^2 R}{(1.655 V_m)^2 R} = 99.85\%$$

b. Form factor:

$$FF = \frac{1.655 V_m}{1.654 V_m} = 1.0008$$

c. Ripple factor:

$$RF = \sqrt{\left(\frac{V_L}{V_{dc}}\right)^2 - 1} = \sqrt{FF^2 - 1}$$

$$= 4\%$$

e.  $V_m$  = peak line to neutral voltage But  $V_{dc} = 1.654 V_m = 280.7 \text{ V}$

$$\Rightarrow V_m = \frac{280.7}{1.654} = 169.7 \text{ V}$$

**PIV** = peak inverse value of secondary line to line voltage  
 $= 169.7 \times 3 = 293.9 \text{ Volt}$

e. The average diode current  $I_{dc}$  is given by:

$$I_{dc} = \frac{2 \times 2}{2\pi} \int_0^{\pi/6} I_m \cos \omega t \, d(\omega t)$$

$$I_{dc} = \frac{2I_m}{\pi} \sin\left(\frac{\pi}{3}\right) = 0.318 I_m$$

If the average load current is  $I_{dc}$  and each diode is on for  $120^\circ$  of a cycle of  $360^\circ$  then average diode current =  $1/3 \times$  average load current

$$I_d = \frac{I_{dc}}{3} = \frac{60}{3} = 20 \text{ A}$$

$$\therefore I_m = \frac{20}{0.318} = 62.83 \text{ A}$$

**W.1** The single-phase full wave rectifier has a purely resistive load of  $R$ , determine:

a) The efficiency,

b) The ripple factor  $RF$ ,

c) The peak inverse voltage PIV of diode NOTE: Drive any formula that used in solution

**W.2** The single-phase half wave rectifier has R-L load with  $R= 5\Omega$  and  $L= 6.5\text{mH}$ . The input voltage  $V_s=220\text{V}$  at  $50\text{Hz}$ , determine:

a) The average diode current

b) The rms diode current

c) The rms output current

d) The average output current

NOTE: Drive any formula that used in solution

**H.W3** The single-phase full wave rectifier has a purely resistive load of  $R$ , and  $I_L=10\text{A}$  and average power =  $100\text{Watt}$ , determine:

-The efficiency,

-The form factor and ripple factor,

-The peak inverse voltage PIV of diode, NOTE: Drive any formula that used in solution

**H.W4** The diode in the single-phase half wave rectifier has a reverse recovery time of  $t_{rr}= 150\mu\text{sec}$  and the source voltage  $V_s= 200\text{V}$  at frequency =  $5\text{kHz}$ . Calculate the average output voltage.

**H.W5:** Design the single phase half wave rectifier supply the HeNe laser tube. The voltage across tube is  $1.8\text{kV}$  and the current pass through tube is  $10\text{mA}$ . The designer has two diodes with PIV= $1.5\text{kV}$  and saturation current are  $I_{s1}=100\mu\text{A}$  and  $I_{s2}=120\mu\text{A}$  respectively.